

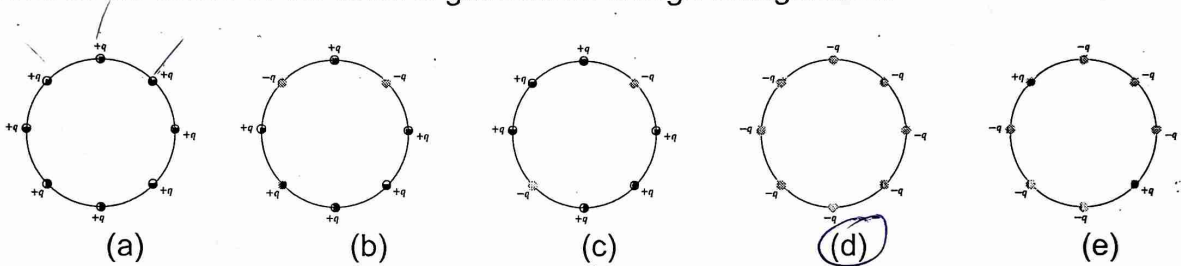
2022

- 1) Suppose the electric potential due to a given charge distribution can be written in Cartesian coordinates as $V(x, y, z) = x^2 - y^2 + z$ volts. The associated electric field at the point $(1.0, 1.0, 1.0)$ m is

- (a) $-2.0 \hat{i} - 2.0 \hat{j} + 1.0 \hat{k}$ N/C
 (b) $-1.0 \hat{i} - 1.0 \hat{j} + 1.0 \hat{k}$ N/C
 (c) $-2.0 \hat{i} + 2.0 \hat{j} - 1.0 \hat{k}$ N/C
 (d) $1.0 \hat{i} + 1.0 \hat{j} + 1.0 \hat{k}$ N/C
 (e) $2.0 \hat{i} - 2.0 \hat{j} + 1.0 \hat{k}$ N/C

~~$\vec{E} = -\nabla V$~~
 $V = \frac{x^2}{1} - \frac{y^2}{1} + \frac{z^1}{1}$
 $V = 2x - 2y + z$
 $\vec{E} = 2\hat{i} - 2\hat{j} + 1\hat{k}$

- 2) Eight charges are equally spaced on a circle of radius R . The magnitude of the electric field at the center of the circle is greatest for charge configuration:



- 3) Two electrons are fixed 4.00 cm apart. Another electron is shot from infinity and stops midway between the two. Its initial speed is

- (a) 80.0 m/s
 (b) 25.0 m/s
 (c) 160 m/s
 (d) 225 m/s
 (e) 500 m/s



- 4) The following charges on an object are physically possible, except

- (a) 8×10^{-21} C.
 (b) 8×10^{-19} C.
 (c) 8×10^{-17} C.
 (d) 8×10^{-15} C.
 (e) 8×10^{-13} C.

$e = 1.6 \times 10^{-19}$

$$F = qE \quad q = \frac{2b}{m} =$$

$$ma = qE$$

- 5) A particle that has a mass of 0.50 g and carries a charge of 5.00 μC is placed in a region in which the electric field is given by $\vec{E} = (1.00 + 4.00x^3) \frac{\text{N}}{\text{C}}$. If the particle starts at rest at $x = 0$, then its speed when it reaches position $x = 2.00 \text{ m}$ is

- (a) 0.03 m/s
 (b) 0.15 m/s
 (c) 0.40 m/s
 (d) 0.18 m/s
 (e) 0.60 m/s

5×10^{-4} ✓

$5 \times 10^{-6} \text{ C}$ ✓

$F = qE$

$x=0 \rightarrow E = 1 \text{ N/C}$

$x=2 \rightarrow E = 33 \text{ N/C}$

$\sqrt{F^2} = \sqrt{v_1^2 + 2q \Delta x}$

$= (2) \quad (2)$

$\frac{1}{2} m v^2 = \dots$

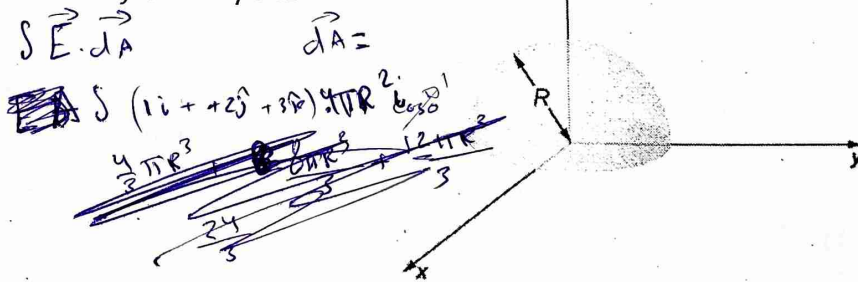
- 6) Two charged particles are arranged as shown. In which region could a third particle, with charge +1 C, be placed so that the net electrostatic force on it is zero



- (a) I only
 (b) II only
 (c) III only
 (d) I and II only
 (e) I and III only

- 7) The electric field flux through the open hemispherical (نصف كرة) surface due to the uniform electric field $\vec{E} = \hat{i} + 2\hat{j} + 3\hat{k} \text{ N/C}$ is

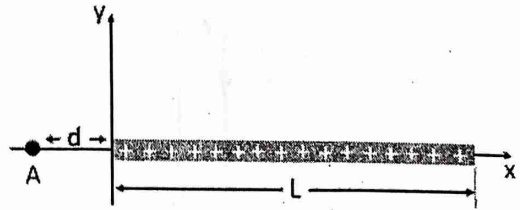
- (a) πR^2
 (b) $2\pi R^2$
 (c) $3\pi R^2$
 (d) $4\pi R^2$
 (e) 0



- 8) The electric potential of an object made from a conducting material is

- (a) greatest at its surface.
 (b) greatest at its center.
 (c) lowest at its surface.
 (d) lowest at its center.
 (e) constant.

- 9) A thin plastic rod of length L lying on the x axis and has a nonuniform positive linear charge density $\lambda = x \times 10^{-9} \text{ C/m}$. If $L = d = 10.0 \text{ cm}$, the electric field at point A is



- (a) $1.7 \hat{j} \text{ N/C}$
 (b) $2.3 \hat{i} \text{ N/C}$
 (c) $-1.7 \hat{i} \text{ N/C}$
 (d) $-3.2 \hat{i} \text{ N/C}$
 (e) 0

Handwritten work for problem 9:

$$E = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2}$$

$$\lambda = \frac{q}{L}$$

$$q = L\lambda$$

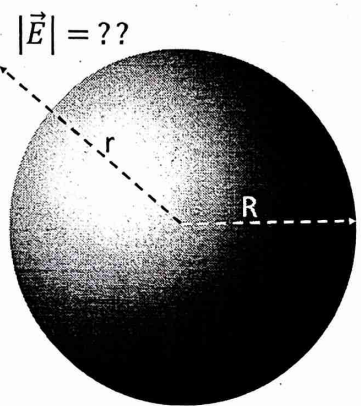
$$E = \int \frac{1}{4\pi\epsilon_0} \frac{\lambda(x) dx}{r^2}$$

$$E = \int_0^L \frac{1}{4\pi\epsilon_0} \frac{x \times 10^{-9} dx}{x^2}$$

$$E = \frac{10^{-9}}{4\pi\epsilon_0} \int_0^L \frac{1}{x} dx$$

$$E = \frac{10^{-9}}{4\pi\epsilon_0} \ln\left(\frac{L}{0}\right)$$

- 10) The magnitude of the electric field outside a non-conducting sphere of radius R that has a volume charge distribution that varies with radial distance r as given by $\rho(r) = \rho_0 \left(1 - \frac{4r}{3R}\right)$

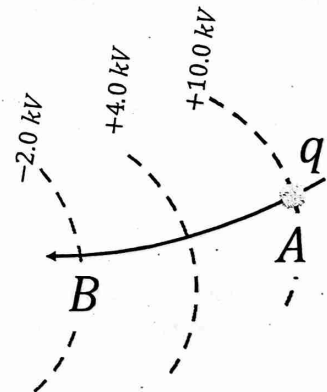


- (a) $\frac{\rho_0 r^2}{\epsilon_0 R} \left(1 - \frac{4r}{3R}\right)$
 (b) $\frac{\rho_0 R^2}{\epsilon_0 r} \left(1 - \frac{r}{R}\right)$
 (c) $\frac{\rho_0 r^2}{4\pi\epsilon_0 R} \left(1 - \frac{4r}{3R}\right)$
 (d) 0
 (e) $\frac{\rho_0 r^2}{\epsilon_0} \left(1 - \frac{16r^2}{9R^2}\right)$

Handwritten work for problem 10:

$$Q = \frac{\rho}{3} 4\pi R^3$$

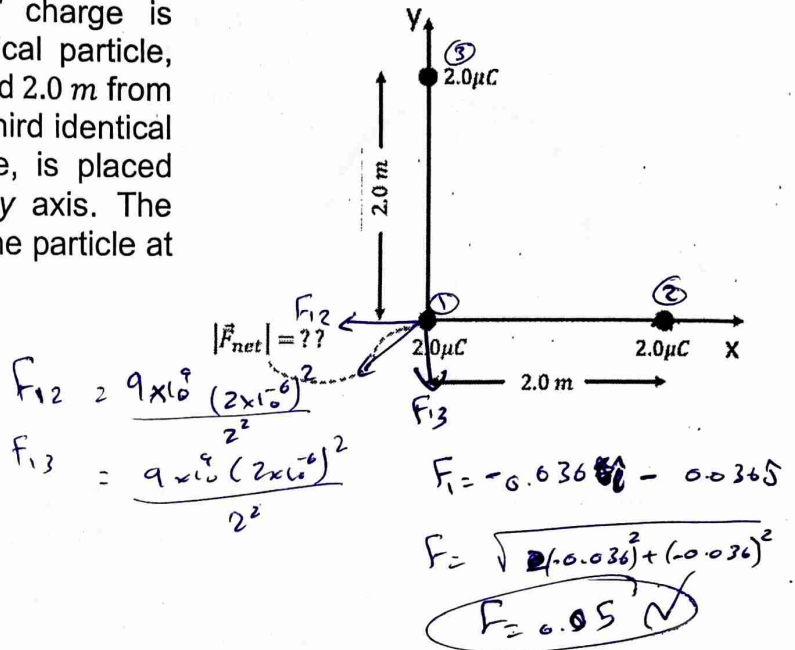
- 11) A particle with charge $+1.5 \text{ nC}$ and mass $1.0 \mu\text{g}$ is released from rest at point A and accelerates for a distance of 2.4 m to point B by moving through the equipotentials shown. The velocity of the particle at B is



- (a) 15 m/s
 (b) 6.0 m/s
 (c) 3.0 m/s
 (d) 2.0 m/s
 (e) 13 m/s

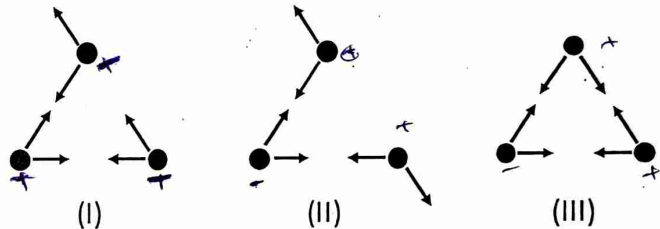
- 12) A particle with charge $2.0\mu\text{C}$ is placed at the origin. An identical particle, with the same charge, is placed 2.0 m from the origin on the x axis, and a third identical particle, with the same charge, is placed 2.0 m from the origin on the y axis. The magnitude of the net force on the particle at the origin is

- (a) $9.0 \times 10^{-3}\text{ N}$
 (b) $6.4 \times 10^{-3}\text{ N}$
 (c) $1.8 \times 10^{-2}\text{ N}$
 (d) $1.3 \times 10^{-2}\text{ N}$
 (e) $1.4 \times 10^{-3}\text{ N}$



- 13) The following diagrams represent the forces that three charged objects might exert on each other, except

- (a) I
 (b) II
 (c) III
 (d) II and III
 (e) None



- 14) An electric dipole of dipole moment $\vec{p} = p_0\hat{j}$ is placed in a uniform electric field $\vec{E} = E_0\hat{i}$. The value of the torque applied on the dipole by the electric field is

- (a) zero
 (b) $p_0E_0\hat{k}$
 (c) $-p_0E_0\hat{i}$
 (d) $p_0E_0\hat{j}$
 (e) $-p_0E_0\hat{k}$

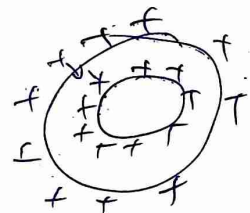
$$\tau = \vec{p} \times \vec{E}$$

$$= p_0\hat{j} \times E_0\hat{i}$$

$$= -p_0E_0\hat{k}$$

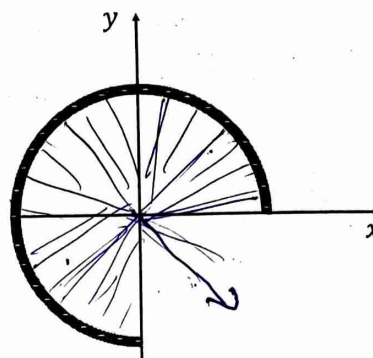
- 15) Consider a closed Gaussian surface that has a positive flux. If a second closed Gaussian surface is completely inside the first one and has a smaller positive charge, then

- (a) There is a negative charge between the two surfaces.
 (b) There is a positive charge between the two surfaces.
 (c) There is a positive charge outside the first surface.
 (d) There is a negative charge outside the first surface.
 (e) There is a negative charge inside the second surface.



- 16) Consider the negative linear, uniform charge distribution shown in the figure. The angle of the electric field vector at the origin with the positive x-axis is

- (a) 90°
 (b) -45°
 (c) -135°
 (d) 45°
 (e) 135°



- 17) A charge Q is distributed uniformly throughout a sphere of radius R . The magnitude of the electric field at a point $R/3$ from the center is

- (a) $\frac{1}{4\pi\epsilon_0} \frac{Q}{R^2}$
 (b) $\frac{1}{8\pi\epsilon_0} \frac{Q}{R^2}$
 (c) $\frac{1}{12\pi\epsilon_0} \frac{Q}{R^2}$
 (d) $\frac{1}{16\pi\epsilon_0} \frac{Q}{R^2}$
 (e) $\frac{1}{24\pi\epsilon_0} \frac{Q}{R^2}$

~~$\frac{1}{4\pi\epsilon_0} \frac{Q}{R^2}$~~ ~~$\frac{1}{8\pi\epsilon_0} \frac{Q}{R^2}$~~ ~~$\frac{1}{12\pi\epsilon_0} \frac{Q}{R^2}$~~ ~~$\frac{1}{16\pi\epsilon_0} \frac{Q}{R^2}$~~ ~~$\frac{1}{24\pi\epsilon_0} \frac{Q}{R^2}$~~

- 18) Two conducting spheres are far apart. The smaller sphere carries a total charge of Q . The larger sphere has a radius that is three times that of the smaller sphere and is neutral. After the two spheres are connected by a conducting wire, the charges on the larger and smaller spheres, respectively, are:

- (a) $Q/2$ and $Q/2$
 (b) $3Q/4$ and $Q/4$
 (c) $2Q/3$ and $Q/3$
 (d) zero and Q
 (e) $2Q$ and $-Q$

